

A ball of mass $m = 0.08$ kg, starting at rest, is dropped from a height $h_1 = 3.0$ meters above the ground and bounces back up to a height $h_2 = 2.0$ meters. The collision with the ground occurs over a time of $.005$ seconds.

a. what is the momentum of the ball immediately before it hit the ground?

Solution:

The momentum of the ball before it hit the ground = $m v_1$

$$v_1^2 = u^2 + 2gs \text{ (Since the ball is dropped } u = 0)$$

$$v_1^2 = 2 \times 9.8 \times 3 = 58.8$$

$$v_1 = 7.6 \text{ m/s}$$

$$\text{Momentum } p_1 = 0.08 \times 7.6$$

$$= -0.614 \text{ kg m/ s}$$

(The momentum is pointing downwards, so Negative)

b. what is the momentum of the ball immediately after it hit the ground?

Solution:

The momentum of the ball after hit the ground = $m v_2$

$$v_2^2 = u^2 + 2gs$$

$$0 = u^2 - 2gs \text{ (since 'g' is negative)}$$

$$u^2 = 2gs = 2 \times 9.8 \times 2$$

$$= 39.18$$

$$u = 6.26 \text{ m/s}$$

$$\text{Momentum } p_2 = 0.08 \times 6.26$$

$$= +0.501 \text{ kg m/s (The momentum is pointing upwards, so Positive)}$$

c. what is the average force of the ground on the ball?

Solution:

Average Force $F = \text{Change in momentum} / \Delta t$

Since p_1 is acting downwards it posses negative sign.

$$F = p_2 - (-p_1) / \Delta t$$

$$F = p_2 + p_1 / \Delta t$$

$$F = (0.501 + 0.614) / 0.005$$

$$F = 1.115 / 0.005$$

$$F = 223 \text{ N}$$

d. what impulse is imparted to the ball during its collision with the ground?

Solution:

Impulse = Change in linear momentum

$$I = p_2 - (-p_1)$$

$$I = p_2 + p_1$$

$$I = (0.501 + 0.614)$$

$$I = 1.115 \text{ kg m/s}$$

e. how much energy is lost during the collision with the ground?

Energy lost = Change in Kinetic energy before and after collision

$$= \frac{1}{2} m (V_2^2 - V_1^2)$$

$$= \frac{1}{2} 0.08 (6.26^2 - 7.6^2)$$

$$= - 0.786 \text{ Joules}$$

Negative sign indicates lost in kinetic energy